

# Hole Mobility Limits for Amorphous and Nanocrystalline Silicon Solar Cells

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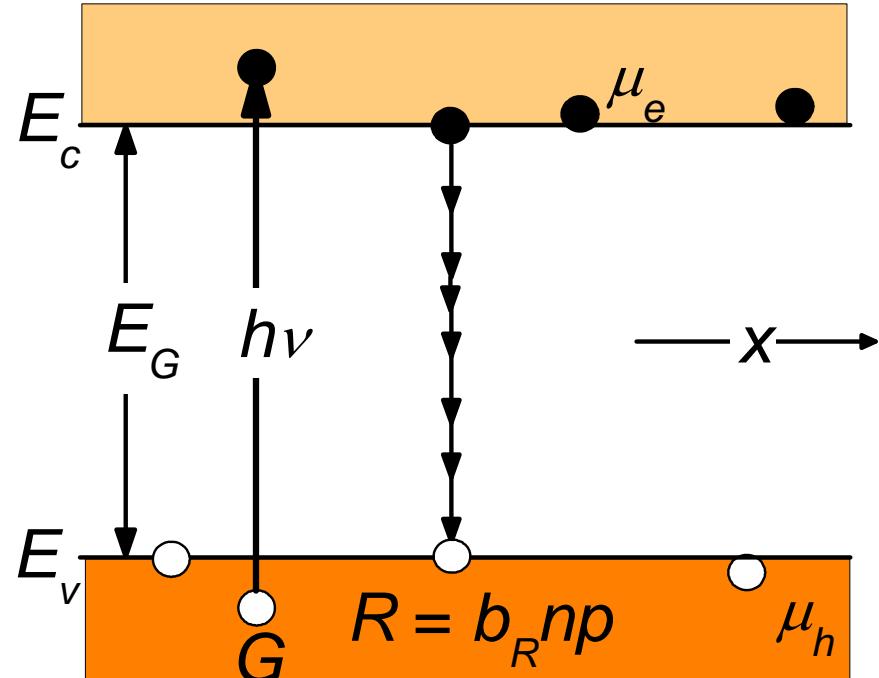
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Baojie Yan, Jeff Yang

Syracuse: Steluta Dinca, Jianjun Liang

# Themes of this Presentation

- Describe “minority carrier mobility limitation” concept for *pin* solar cells
  - For low-mobility absorbers, the magnitude of recombination parameters can have very little effect.
- Describe experimental testing of hole mobility limited description for United Solar Ovonic Corp.’s a-Si:H solar cells Answer “what if” questions about initial state of a-Si:H and nc-Si:H solar cells:
  - improve mobility? reduce recombination?
  - Why are nc-Si:H solar cells about 2 microns thick?
- Apply description to the light-soaking problem
  - Modest defect recombination plays well with H-collision.
  - Suggests that light-soaking in United Solar Ovonic cells is *self-limiting*

# Low-mobility *pin* Solar Cells: “Toy” Model and Analytical Solution

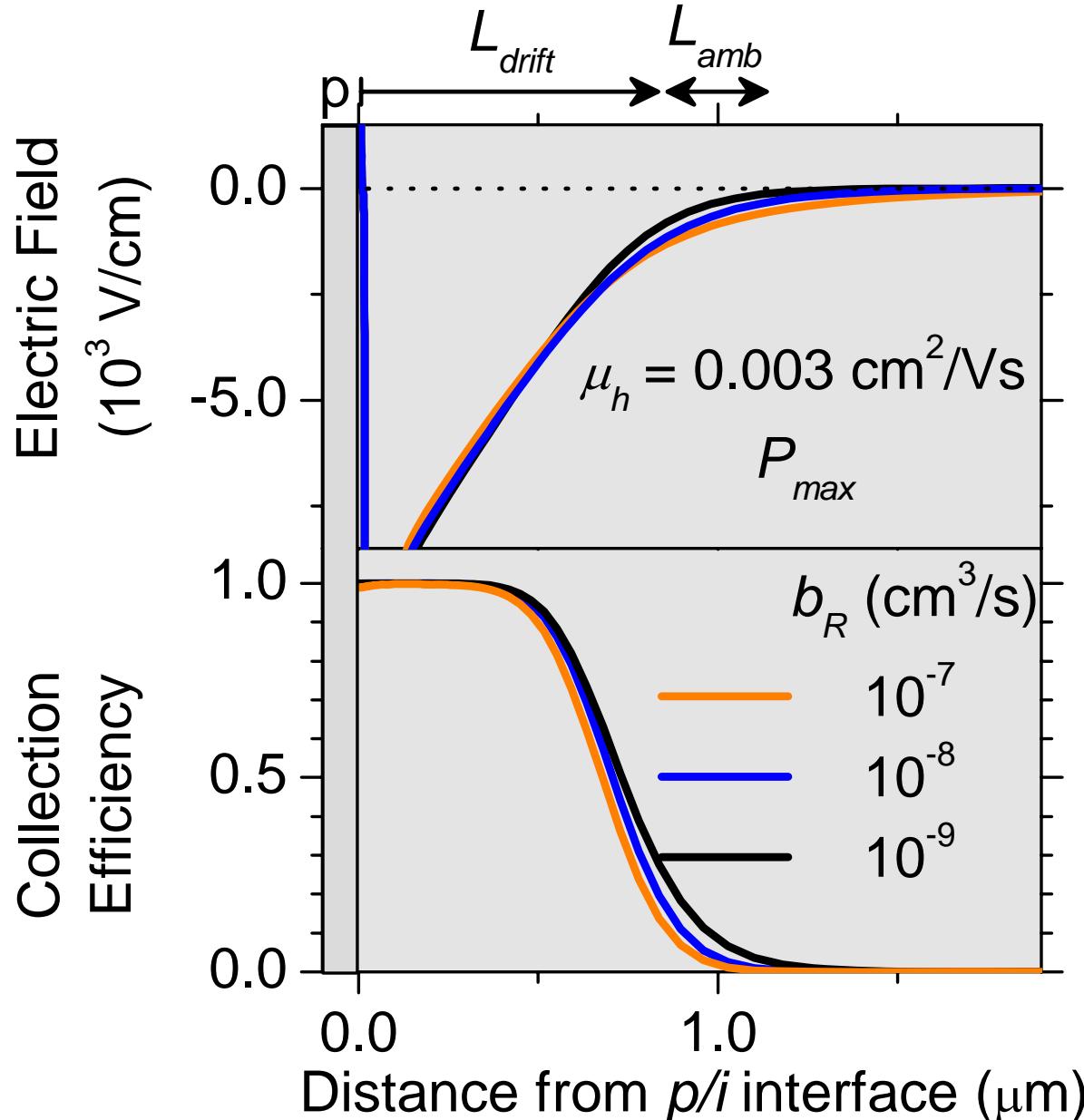


$$P_{\max} = \left( \mu_h \varepsilon (eG)^3 \right)^{1/4} \left( (2/3)V_{OC} \right)^{3/2}$$

$$\mu_e \gg \mu_h$$

$$eV_{OC}^0 = E_G + kT \ln \left( \frac{G}{b_R N_C N_V} \right)$$

# Recombination Effects on a Low-mobility *pin* Solar Cell

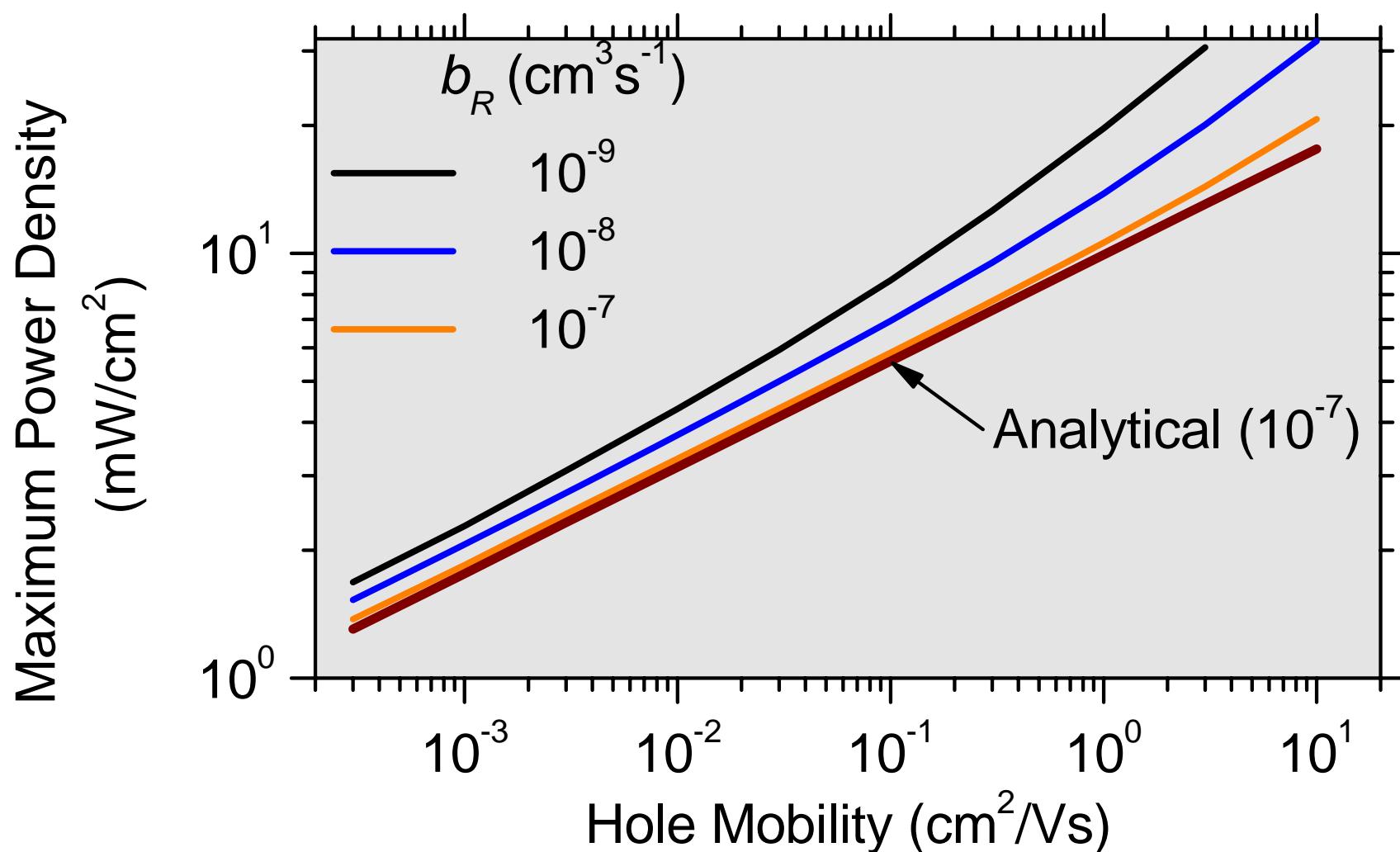


Computer Calculations

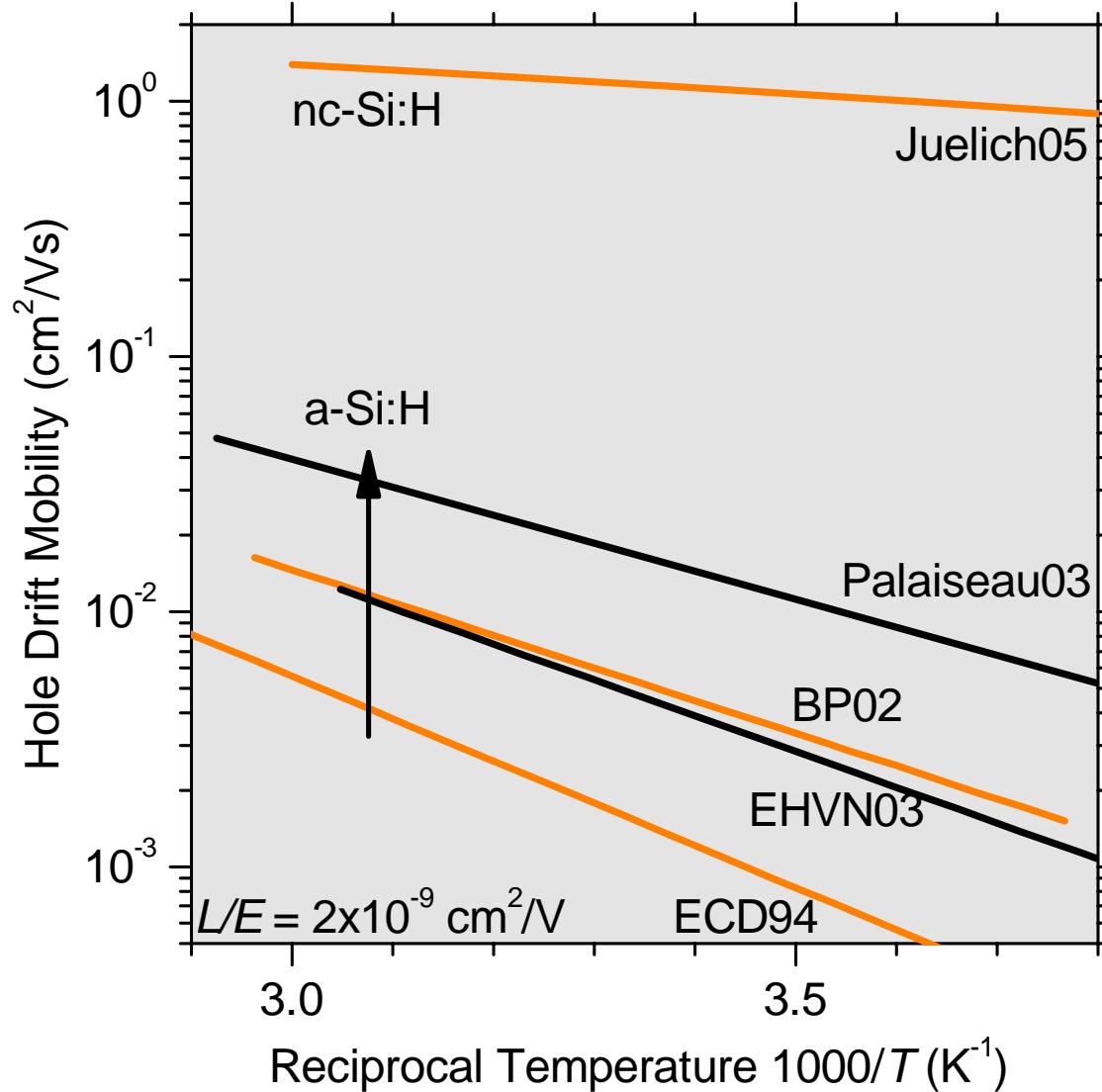
$L_{drift}$ : width of space charge layer

$L_{amb}$ : ambipolar diffusion length  
(shown for  $b_R = 10^{-9} \text{ cm}^3/\text{s}$ )

# Mobility Is Power: Computer and Analytical Calculations



# Hole Drift-Mobilities in Disordered Silicons

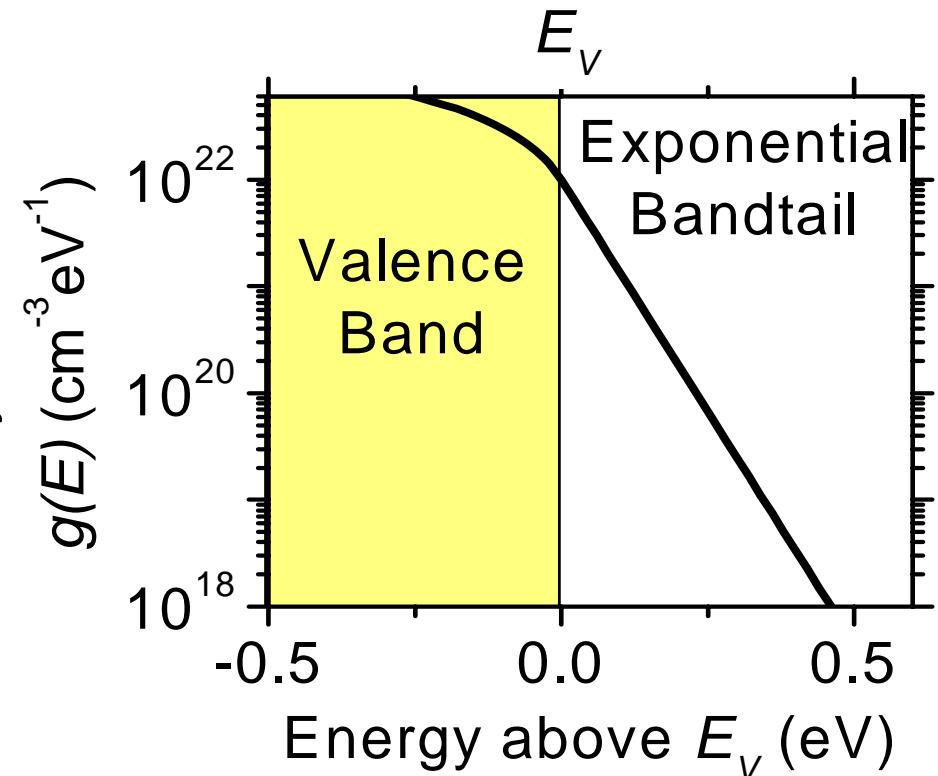


E. A. Schiff, *J. Non-Cryst. Solids*, in press (ICANS 2005).

nc-Si:H - T. Dylla, F. Finger, and E. A. Schiff, *Appl. Phys. Lett.* **87**, 032103 (2005) [[pdf](#)].

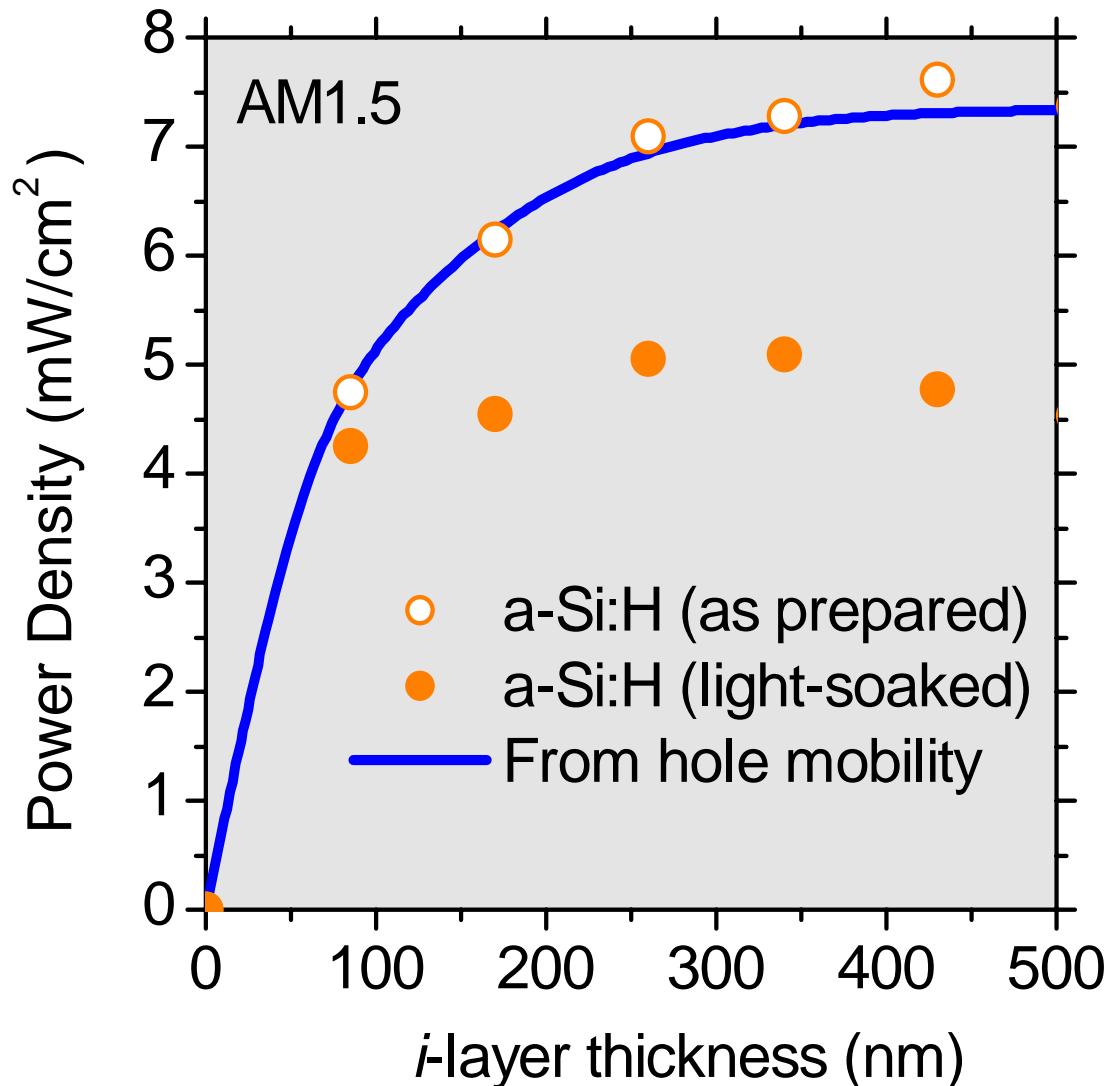
E. A. Schiff, *J. Phys.: Condens. Matter* **16**, S5265-5275 (2004) [[pdf](#)].

# Bandtail Multiple-Trapping Model for Hole Drift Mobility



Bandtail Parameters	
$\Delta E_v$	Valence Bandtail Width
$\mu_h$	Hole Band Mobility
$N_V b_T$	Attempt Frequency

# Power Density in (simple) United Solar Ovonic Cells

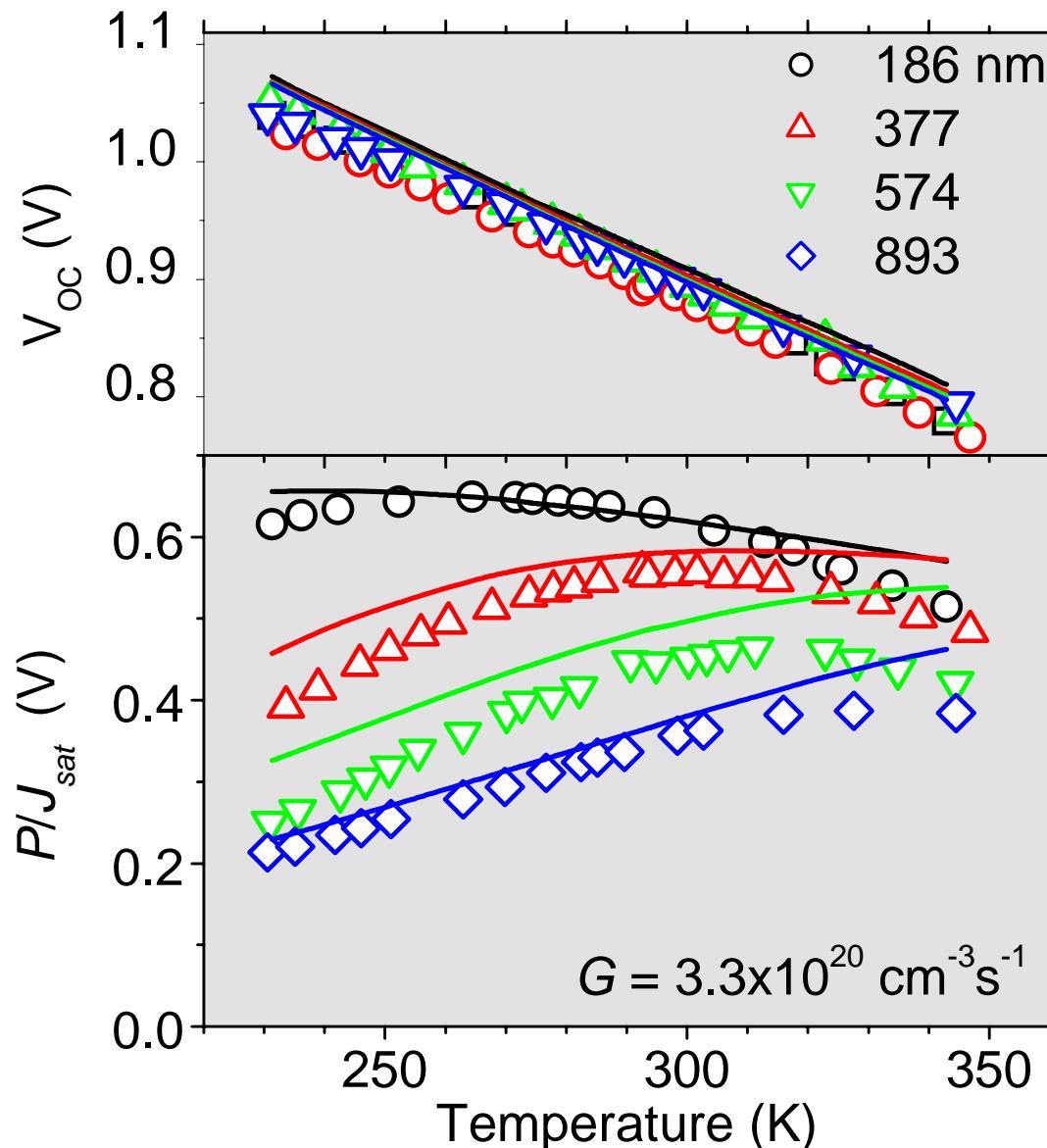


## Model Parameters

$\mu_p$	0.3 cm <sup>2</sup> /Vs
$\Delta E_v$	0.040 eV
$N_v, N_c$	$4 \times 10^{20} \text{ cm}^{-3}$
$b_T$	$1.3 \times 10^{-9} \text{ cm}^3 \text{s}^{-1}$
$E_g$	1.74 eV
$b_R$	$1.0 \times 10^{-9} \text{ cm}^3 \text{s}^{-1}$

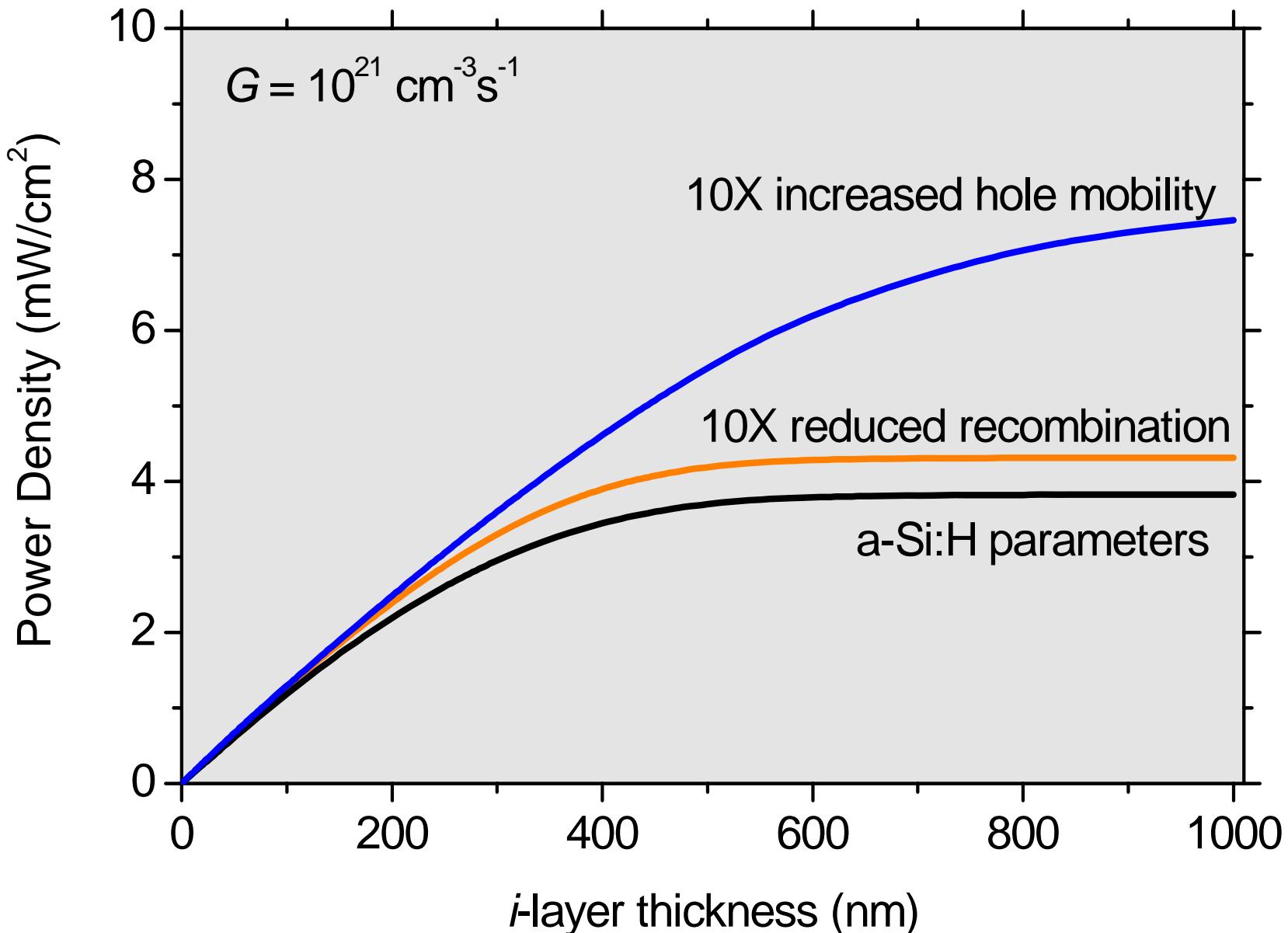
No defects. Ideal  $p, n$ .  
Other parameters are less important

# Power Density vs. Temperature, Uniform Generation: A Better Test for Mobility Limitation

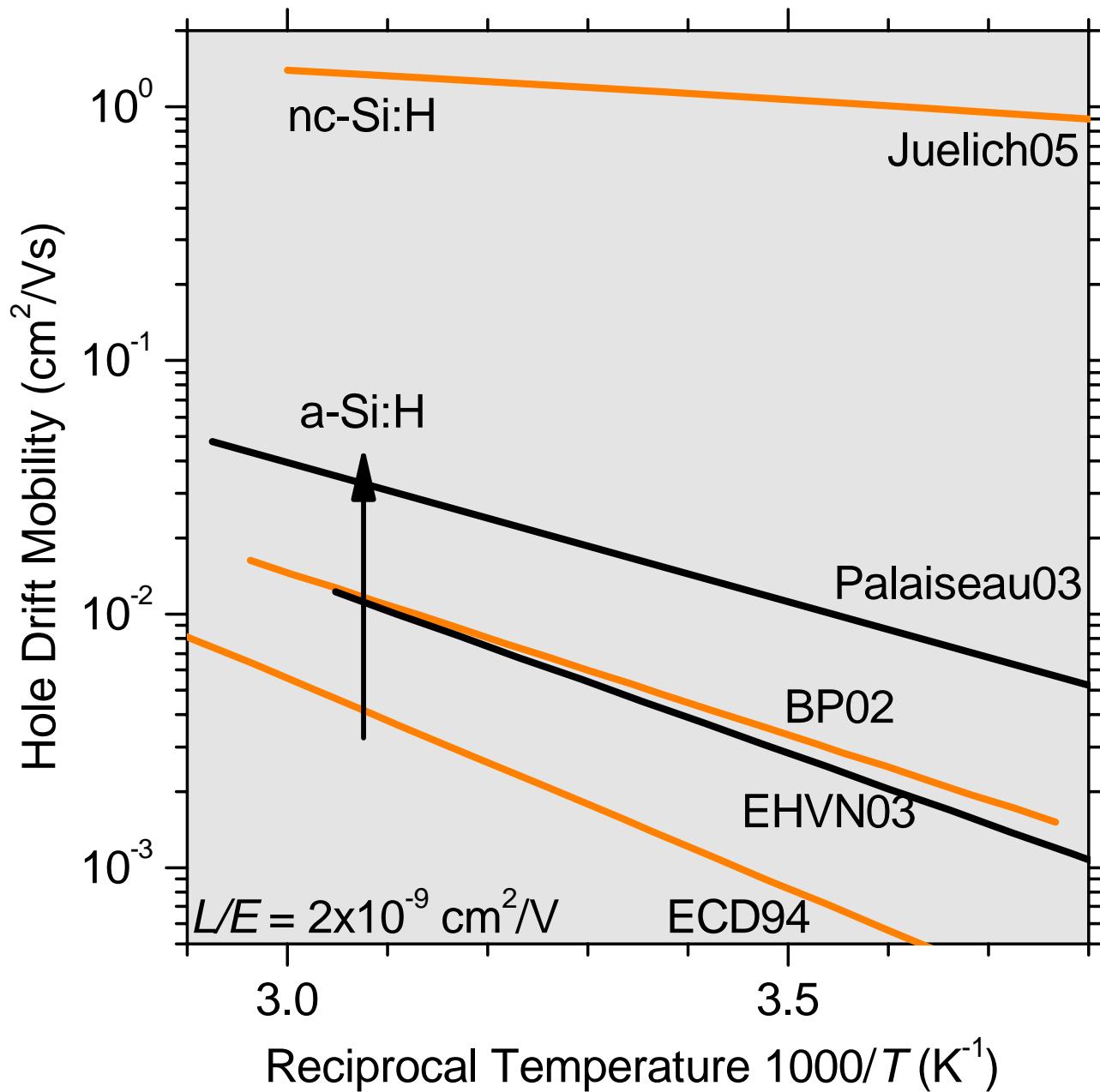


Model Parameters	
$\mu_p$	$0.3 \text{ cm}^2/\text{Vs}$
$\Delta E_v$	$0.040 \text{ eV}$
$N_v, N_c$	$4 \times 10^{20} \text{ cm}^{-3}$
$b_T$	$1.3 \times 10^{-9} \text{ cm}^3\text{s}^{-1}$
$E_g$	$1.74 \text{ eV}$
$b_R$	$1.0 \times 10^{-9} \text{ cm}^3\text{s}^{-1}$

# What if - hole mobility increases?



# Hole Drift-Mobilities in Disordered Silicons



# Nanocrystalline and Crystalline Si Cells

- nc-Si:H absorbers are typically a “few” microns thick, but crystalline silicon absorbers can be 100’s of microns thick. Why the large difference?
- Low-mobility expression for optimum absorber thickness:<sup>1</sup>

$$L_{drift} = ((2/3)V_{oc})^{1/2} (\mu_h \epsilon / eG)^{1/4}$$

- Evaluating for a mobility of  $\mu_h \approx 1 \text{ cm}^2/\text{Vs}$  in nc-Si:H,  $L_{drift}$  for the nc-Si:H absorber is about  $2 \mu\text{m}$ .<sup>2</sup>
  - Agrees pretty well with device makers’ experience
  - nc-Si:H absorbers are close to mobility-limitation.

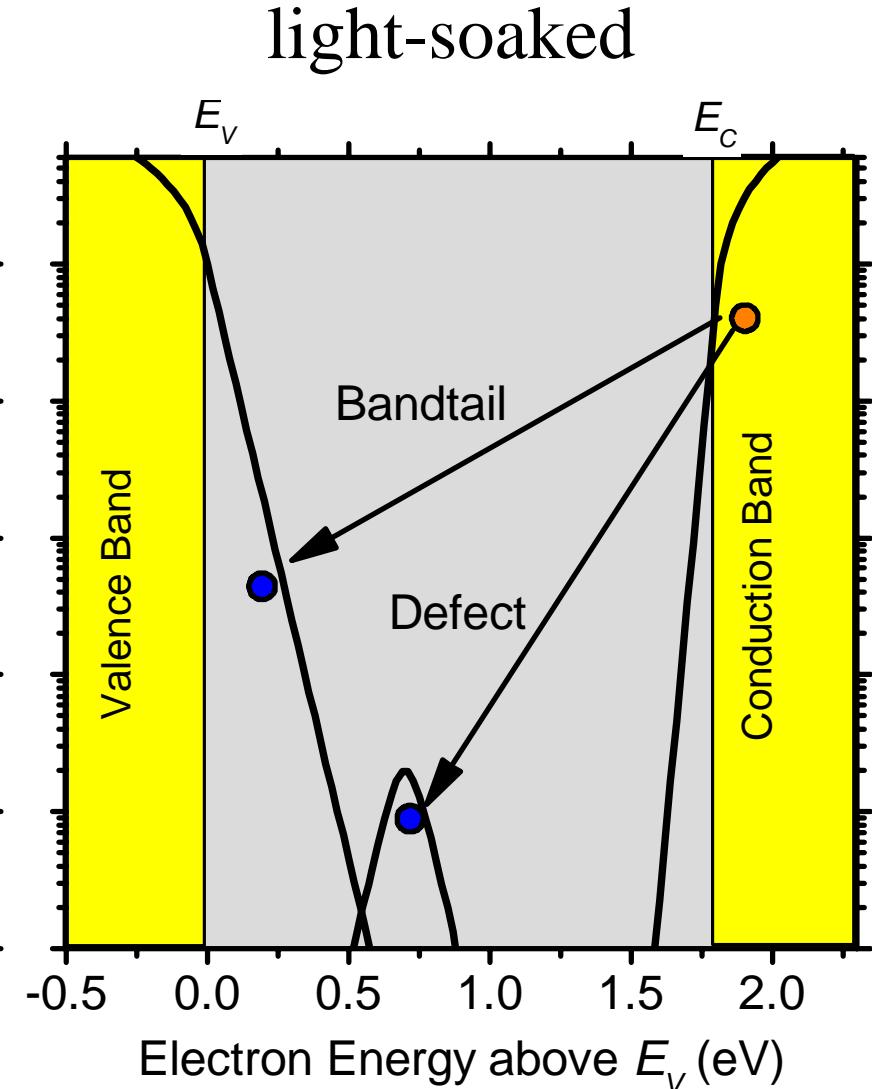
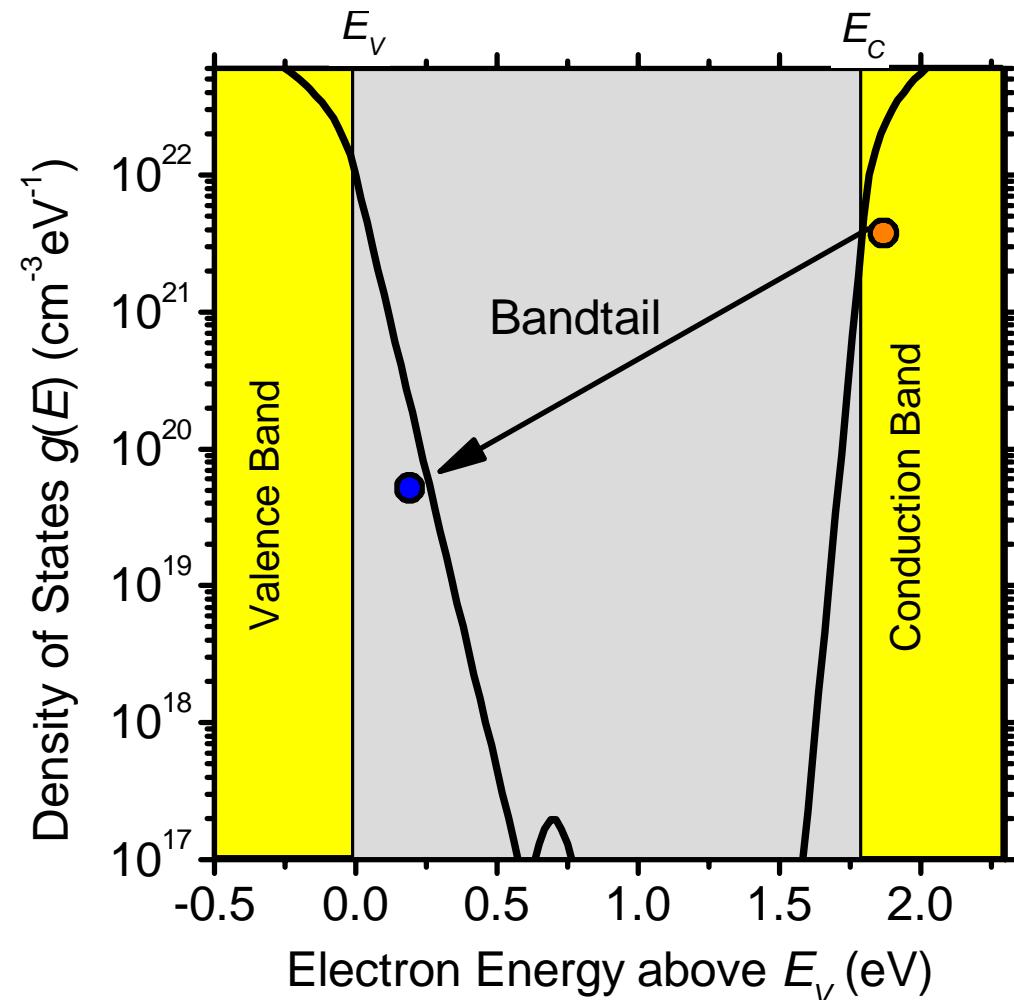
<sup>1</sup>E. A. Schiff, *Solar Cells and Solar Energy Materials* **78**, 567-595 (2003). [[.pdf](#)]

<sup>2</sup>Used  $V_{oc} = 0.6 \text{ V}$ ,  $G = 5 \times 10^{20} \text{ cm}^{-3}\text{s}^{-1}$ .

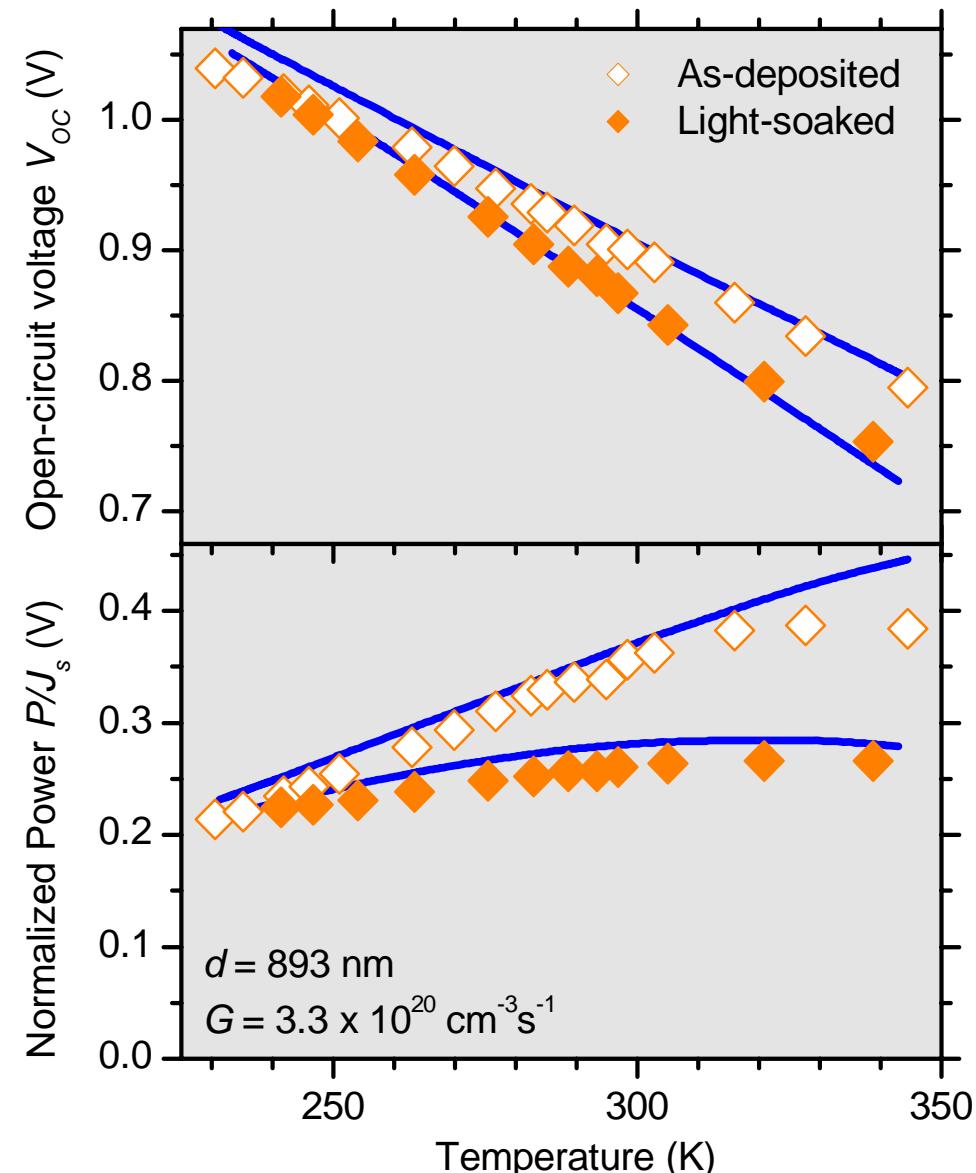
# Recombination & Light-Soaking

as-deposited

light-soaked

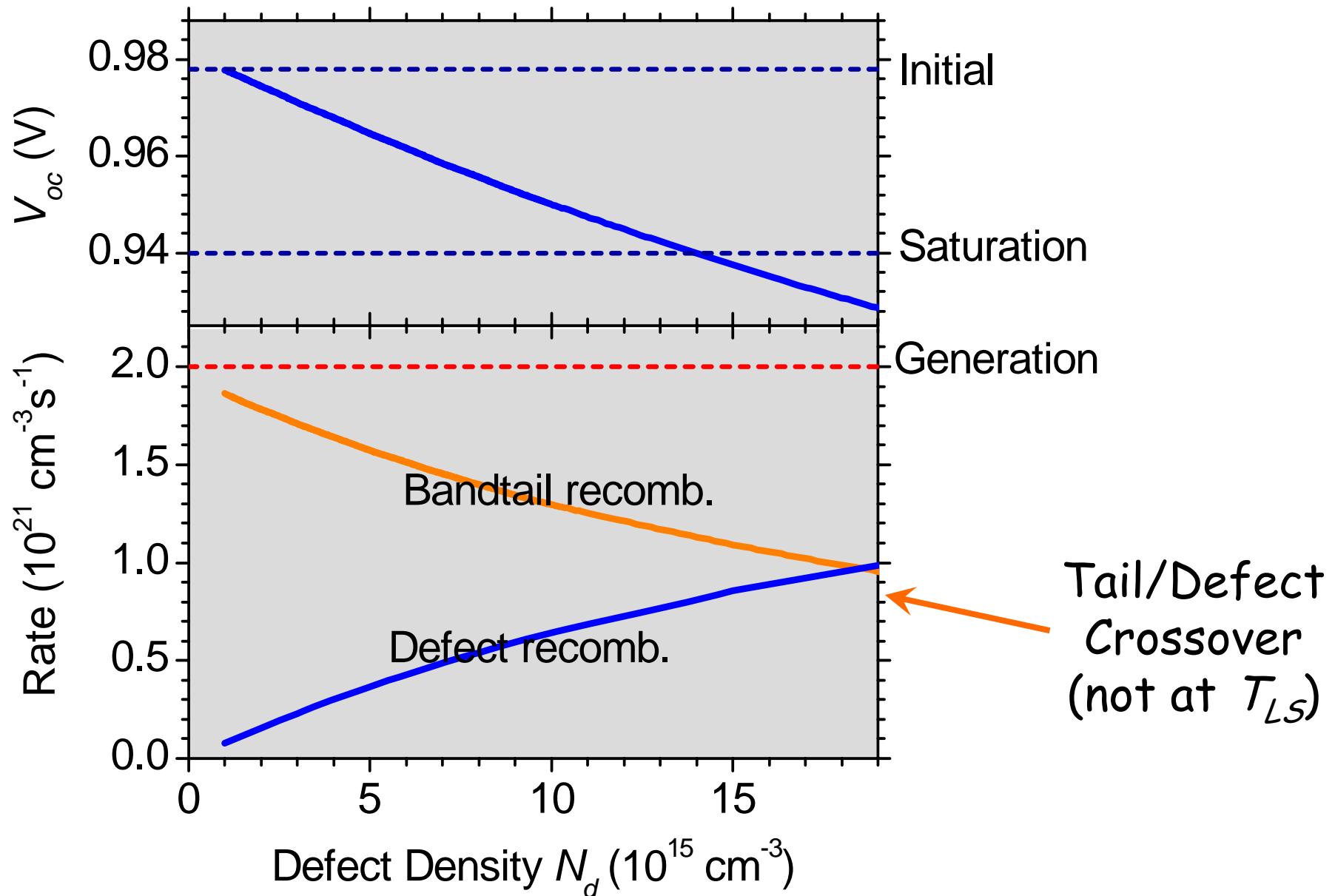


# United Solar Ovonic Cells: Temperature Effects

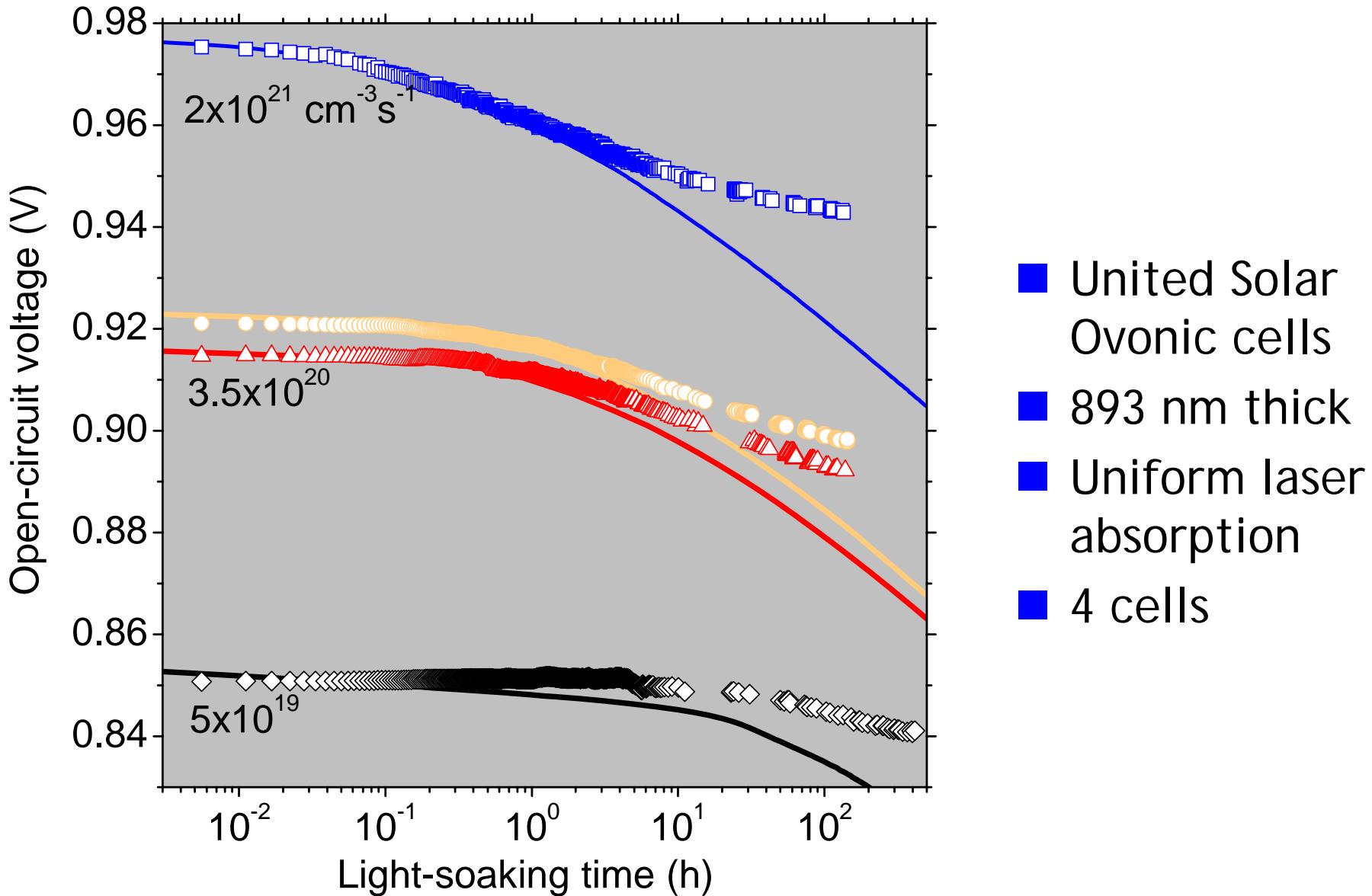


- United Solar Ovonic cells
- 685 nm laser illumination
- Lines are computer calculations
- As-deposited: only bandtails significant
- Light-soaked: bandtail+defect
- Defect density about  $2 \times 10^{16} \text{ cm}^{-3}$
- Defect parameter values from Street's deep-trapping measurements

# Light-Soaking & Bandtail+Defect Model



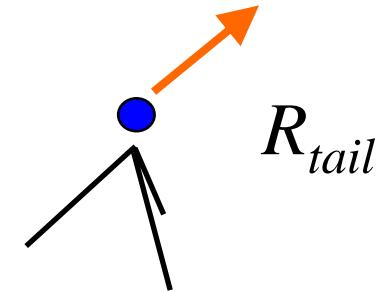
# Measured Light-soaking Kinetics of $V_{OC}$



# Models for Kinetics for $N_d(t)$

H-collision  
(modified)<sup>1,2</sup>

$$\frac{dN_d}{dt} \propto H_m^2 = C_{SW} \left( \frac{R_{tail}}{N_d} \right)^2$$



SJT<sup>3</sup>

$$\frac{dN_d}{dt} = A_{SW} R_{tail}$$

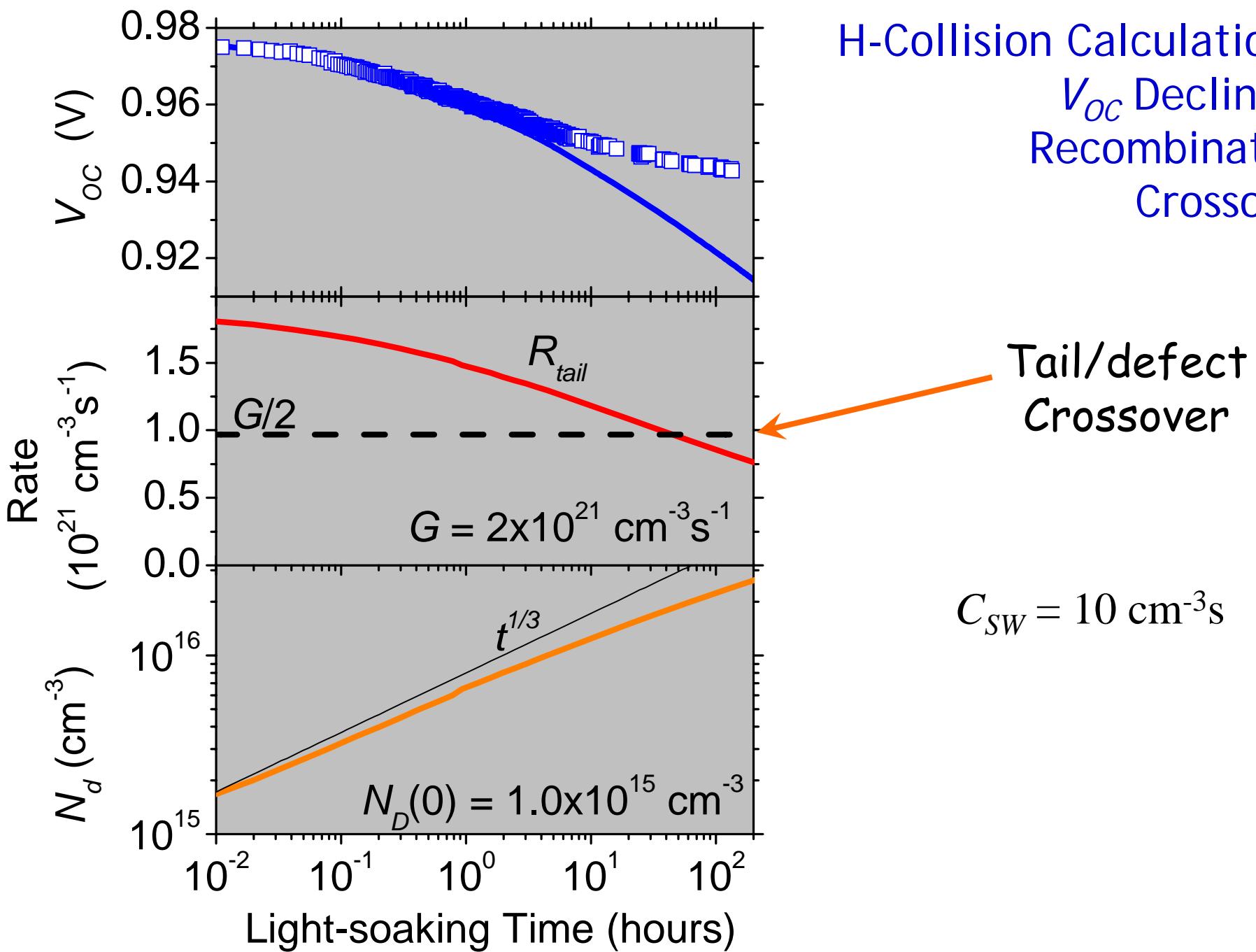
Doesn't account for kinetics  
of these cells

<sup>1</sup>H. M. Branz, *Phys. Rev. B* **59**, 5948 (1999).

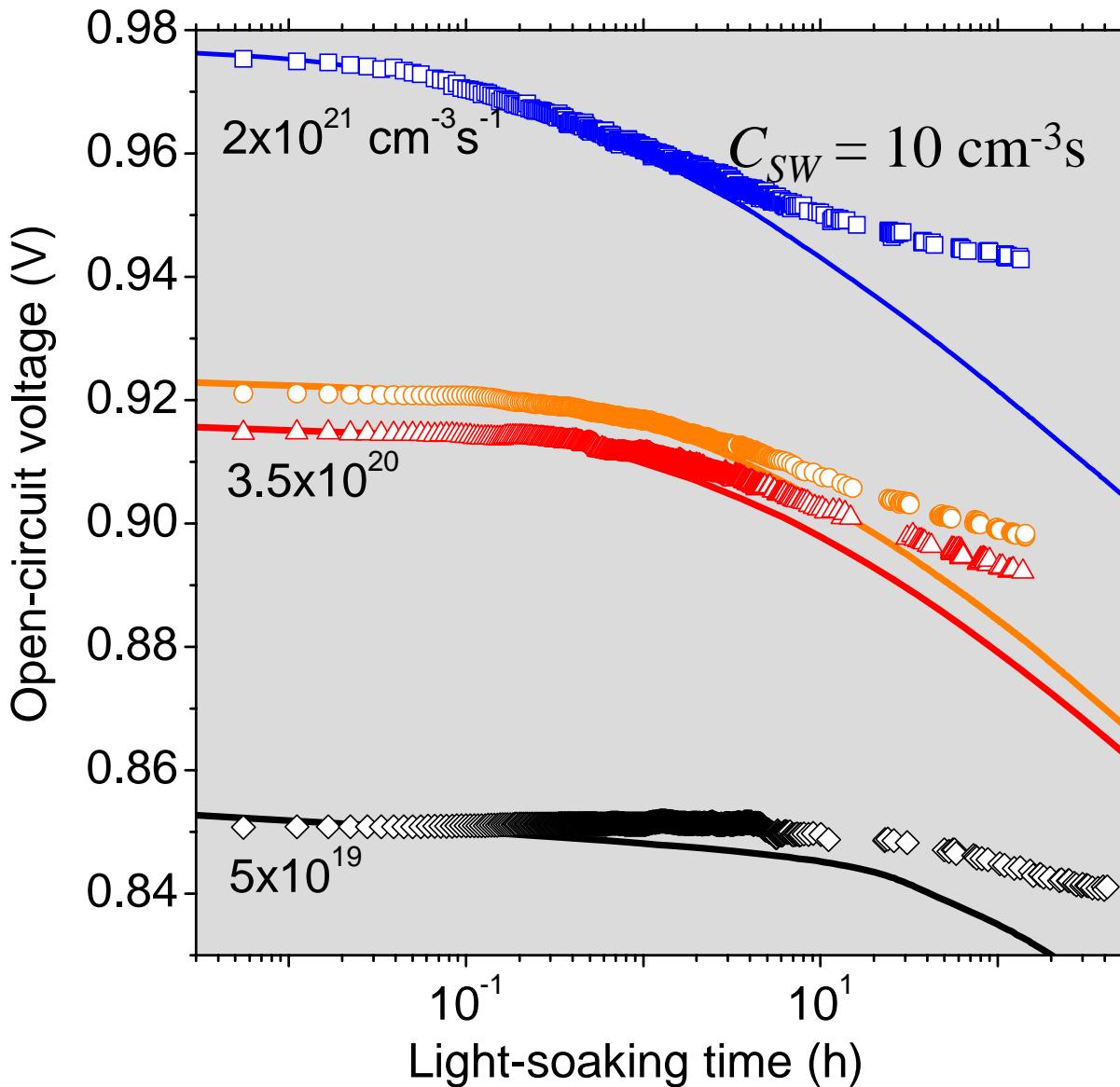
<sup>2</sup>J. Liang, et al., in *Amorphous and Nanocrystalline Silicon Science and Technology – 2005*, edited by R. Collins, (Materials Research Soc. Symp. Proc. Vol. 862, Pittsburgh, 2005), A13.6 [[pdf](#)].

<sup>3</sup>M. Stutzmann, W. B. Jackson, C.-C. Tsai, *Phys. Rev. B* (1985)

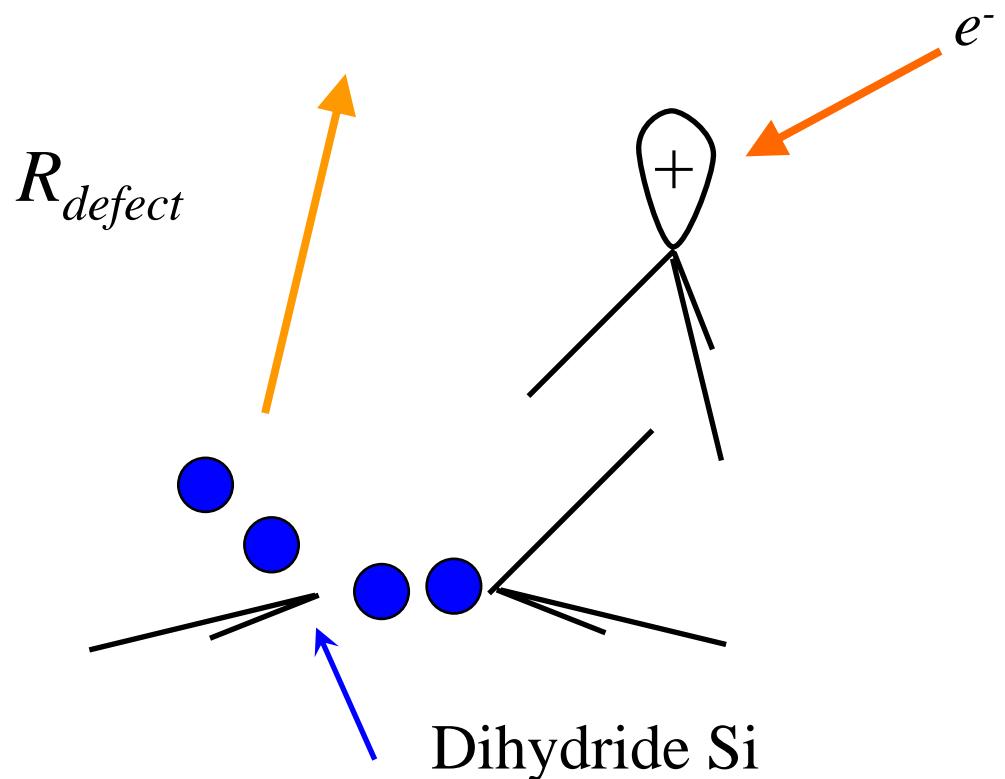
# H-Collision Calculations: $V_{OC}$ Decline & Recombination Crossover



# H-collision Predictions for $V_{OC}(t)$



# Speculation: Light-Soaking is Self Limiting



- Puzzle: Why does light-soaking degrade  $V_{OC}$  and  $P_{max}$  so *little*?
- Speculation: recombination through defects releases H, and anneals defects.

$$\frac{dN_D}{dt} \approx C_{SW} \left( \frac{R_{tail}}{N_D} \right)^2 - D_{LIA} R_D \left( \frac{N_D}{2} \right)$$

# Open Questions & Future Pathways

- Higher power a-Si:H, nc-Si:H cells require better holes
  - Necessary, but not sufficient.
  - Will higher mobility, “polymorphous” materials yield higher efficiency cells?
  - Are a-SiGe cells also mobility-limited?
- Light-soaking of United Solar Ovonic’s material appears to be “self-limiting.”
  - Surprising in the context of some thin-film studies on older materials.
  - How did that happen? Will higher mobility cells still have good light-soaking properties?